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Surbey of India.

DEPARTMENTAL PAPER-No. 7.

THE BAR COMPARISONS OF 1907 AND 1908.

BY

MAJOR H. M. COWIE, R.E., DEPUTY SUPERINTENDENT, SURVEY OF INDIA.

PUBLISHED UNDER THE DIRECTION OF THE SURVEYOR GENERAL OF INDIA.



Dehra Dun: PRINTED AT THE OFFICE OF THE TRIGONOMETRICAL SURVEY.

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PREFACE.

The following pages are based on a report and notes by Major Cowie. Major Cowie was absent on the Turco-Persian Frontier Commission at the time when the paper was being passed through the press, and some discretion had to be used in deciding what should be printed. In some cases the arrangement and wording was slightly altered when this appeared desirable. Minor inconsistencies were removed whenever these were noticed.

Babu Rasik Chandra Ray of the Computing Office scrutinised the copy and read all the proofs.

DEHRA DUN, April, 1915.

J. de GRAAFF HUNTER.

THE BAR COMPARISONS OF 1907 AND 1908.

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During the summer of 1907 the question of adopting the metre as the unit of length in geodetic operations in India was brought prominently forward, and the arguments for and against this step were considered and discussed by the Survey of India and eminent geodesists in England. The immediate cause, which gave rise to this question, was the prospective acquisition by the Survey of India of invar wires for the measurement of bases by the Jäderin method. These wires were to be made and tested at Sévres, where all the apparatus for the construction and the later standardizing of wires is adapted to the metre unit and where customs and procedure have been moulded to suit wires 24 metres in length, this being the length generally adopted by European Geodetic bodies. The Survey of India had to consider whether it would follow European example and use 24-metre wires, or whether, adhering to the 10-foot unit upon which all its past geodetic operations were based, it would provide itself with wires whose length was some multiple of this unit. The former alternative involved difficulties of standardizing the wires from time to time in the field and the referring of base measurements of the future to those of the past. With the latter alternative had to be considered the fact that the Indian 10-foot Bar (made about the year 1830) had now been outclassed by modern standards, both as regards design and construction.also that this standard had already served its purpose as a unit for the Indian Survey and that the time was approaching when this survey* would be linked up with others based on the International Metre as unit. It was finally decided to adopt the metre as the geodetic unit and to use wires of 24 metres length; to procure a new 4-metre standard bar of invart, for the standardizing of these wires whose length should be known in terms of the International Metre; and, to compare the old 10-foot Standard Bar A with the International Metre for the connection of future base measurements with those of the past.

^{*} A connection with Russian Triangulation has been completed in 1913.

[†] A more complete set of standards together with the necessary comparator apparatus has since been acquired.

It is true that there already existed a value of the Indian Standard A in terms of the old metre. This value was not obtained, however, from direct comparisons, but through the sister bar B, the bar I_{s} and the Ordnance Yard, Y_{55} .

The different steps of the deduction are as follows :----

 $l_{s} - B = +86.81$ v

millionths of a yard (later on abbreviated into m.y), determined by Clarke's comparisons in 1865 in England.

$$\mathbf{I}_{s} - \mathbf{A} = +82.52 \ m.y$$

as derived from the observations made between 1867 and 1870 in India. Combining these two values,

$$A = B + 4.29 m.y.$$

$$B = 3.333,315,90 Y_{55}$$
$$A = 3.333,320,19 Y_{55}$$

and hence,

also from Clarke's determinations

$$\mathbf{Y}_{55} = 0.914,391,43 \text{ M}$$

where M represents the old metre.

Whence is derived

$$A = 3.047,959,42$$
 M

and by introducing the value of M in terms of the International Metre, the length of A can be referred to the latter.

There were two objections, however, to adopting the relation between A and the International Metre arrived at as outlined above. One was that many stages were involved in the comparison, each step being a possible source of error. The value of **B** may have been fairly well known in terms of the metre, but to connect **A** with the metre, recourse had to be made to the comparison of both **A** and **B** with the bar I_S . Now **B** was compared with this bar in England in 1865, **A** was compared with it in India in 1867-70. In the interim, the bar had been conveyed from England to India and the observations available offer no data for ascertaining whether the bar was or was not affected by the journey, and whether the absolute length of the bar on its arrival at Dehra Dūn was the same as it had been at Southampton. The value of the relation between **A** and the old metre thus depends, in great measure, on the degree of invariability maintained by the bar I_S during the period 1865-1870. The other point was that the date at which the comparison had been made was so far distant, that it was quite reasonable to doubt whether the relationship then ascertained still held good. It is known that with time metal bars may undergo certain changes which affect their absolute length. The advisability of using for purposes of connecting new geodetic measurements, in terms of one unit, with old work in terms of another, a factor determined 50 years previously and for a metal bar possibly affected by time, was open to doubt.

For these reasons the adoption of 24-metre wires for the measurement of future geodetic bases necessitated the direct comparison of the Standard of India, Bar **A**, with the International Metre. For this purpose, the bar had to be sent to the Pavillon Breteuil at Sévres and, in order that some means should be available for indicating whether the absolute length of the bar had been unaffected or not by its transport, and, if affected, of determining the magnitude of the change, it was advisable that careful comparisons should be made in India both before and after its journey to Europe. These comparisons were made in November, December of 1907 and January of 1908 and in November and December of 1908, the bar in the interval going to Sévres and being compared with the International Metre. The comparisons carried out in India were of the Standard Bar **A** with the cast steel bar I_S and the bar I_B of Baily's metal (an alloy of copper, tin and zinc).

These two bars I_s and I_B were made in 1864 by Messrs. Troughton and Simms. The object of their construction was to settle questions that had been raised as to the possible variation of length which the standard might have suffered in the course of its several journeys from the Survey Head Quarters to the various base lines at which it was used.

Our knowledge of the relative lengths of the three bars was based on the following investigations :---

In 1834 and 1835, the bars **A** and **B** were compared at Dehra Dūn by Sir George Everest. The result he obtained was

 $\mathbf{B} - \mathbf{A} = 1.24 \text{ m.y.}$ afterwards corrected to 0.64 m.y.

This value, however, was not considered a very reliable one, on account of the difficulty there had been of determining the true temperatures of the bars during comparison, by reason both of the particular construction of the thermometers used and the imperfect knowledge of the errors of graduation of their scales.

The value adopted for the absolute expansion of A, in the first discussion of these comparisons, was 22.669 m.y for 1° F. This quantity had been determined by observation at Calcutta in 1832. Further examination of the various comparisons made at the different base lines, between this bar and the Colby compen+

sated bars, showed that this value was probably too large. Further investigations, made in 1870, gave the result $21.797 m.y^*$ which has been employed in the reduction of all later measures made with this bar.

Of the expansion of bar **B** no direct determinations have ever been made. In the reduction of the 1834-35 comparisons, the observation equations were therefore formed to involve two unknown quantities, the difference between the lengths of the bars at 62° F and the difference of their absolute expansions.

These comparisons between bars **B** and **A**, when rediscussed, using the 1870 value of the expansion of **A**, gave the result 0.64 m.y, stated above, as the difference between the lengths of the bars and the quantity -0.153 as the difference in the values of their absolute expansions, making that for **B**, 21.644 m.y.

Clarke, in 1865, made comparisons between the bars B, I_B, I_S, O_1, OI_1 , and Y_{55} , the last three belonging to the Ordnance Survey, and found

$$I_s - B = 86.81 \quad m.y$$

 $I_B - B = 218.27 \quad ,,$

In the reduction of these observations, Clarke assumed that the expansion of **B** was the same as that of O_1 , which had been obtained by comparison with that of O_1 . The absolute expansion of this latter bar was determined by direct experiment. The quantity thus deduced for **B** was $21 \cdot 532 m.y$.

The expansions used for I_B and I_S had been determined simultaneously by direct experiment, in 1865, by Clarke. The values were :---

Expansion of
$$I_B = 32.759 m.y$$

 $I_S = 21.159$,

The combination of Clarke's 1865 determination of the relative lengths of I_s , I_B and **B** with Everest's comparison of **B** and **A** gave the first available values of I_s and I_B in terms of **A**.

From Everest's observations of 1834-35, using the later value of the expansion of **B**, we have

B - A = 0.64 m.y

Clarke's values of 1865 were

$$l_s - B = 86 \cdot 81 \ m.y$$

 $l_B - B = 218 \cdot 27 \ ,$

Hennessey's value of 1870.

from which may be derived

$$I_s - A = 87.45 m.y$$

 $I_B - A = 218.91 ,,$

It is to be noted, however, that in the two series of comparisons, from which these quantities are deduced, slightly different values were allotted to the absolute expansion of bar **B**. In the comparisons with **A** the expansion was assumed to be 21.644 and in those with I_B and I_S the value 21.532 was used.

The first series of direct comparisons between the three bars \mathbf{A} , \mathbf{I}_B and \mathbf{I}_S was carried out in 1867 at Dehra, measurements being made of the differences of length for each pair of bars. In the reduction of the observations the expansions adopted for \mathbf{I}_B and \mathbf{I}_S were those determined by Clarke in 1865 and for \mathbf{A} , the value given by Everest. Thus the following expansions were used :---

Expansion of
$$I_B = 32.759 \text{ m.y per 1}^\circ \text{F.}$$

 $I_S = 21.159 \text{ ,, ,, ,,}$
 $A = 22.669 \text{ ,, ,, ,,}$

and the results of these observations were

$$I_B - I_S = 131 \cdot 40 \ m.y$$

 $I_B - A = 221 \cdot 32 \ ,$
 $I_S - A = 89 \cdot 94 \ ,$

In 1870, Mr. J. B. N. Hennessey undertook the redetermination of the expansions of the bars A and I_s . With this object, a comprehensive series of experiments was carried out at Mussooree, using apparatus adapted from that employed by Clarke in 1864-65. The results of these observations were

expansion of
$$A = 21.797 \text{ m.y per } 1^{\circ} \text{ F.}$$

 $I_{s} = 21.290 \text{ , , , , , , , , }$

This value of the expansion of I_s was then combined with Clarke's determination, 21.159, (resulting from Clarke's second series of observations) and the mean value thus deduced, 21.225, has been adopted in all measurements in which I_s has played a part since 1870. Since that date no further investigations have been made of the absolute expansions of the bars A, I_B and I_s , the following being accepted as final values:—

Expansion of
$$\mathbf{A} = 21.797 \text{ m.y per 1}^{\circ} \mathbf{F}$$
.
 $\mathbf{I}_{s} = 21.225 \text{ , } \text{ , }$
 $\mathbf{I}_{B} = 32.759 \text{ , } \text{ , }$

Using these quantities, the comparisons of 1867 were reconsidered and the values given below deduced.

$$I_s - A = 80.84 m.y$$
 at 62°
 $I_B - A = 212.64 ,, ,,$
 $I_B - I_s = 132.06 ,, ,,$

Further, discussing the expansion experiments of 1870 by themselves, the relation between I_s and **A** was found to be

$$\mathbf{I}_{s} - \mathbf{A} = 84.03 \ m.y.$$

Four series of comparisons have thus been carried out, involving the bars **A**, **B**, I_B and I_S .

Recapitulating, these are :---

No. of comparison	Bars compared	Year	Results
1	B and A	1834-35	$\mathbf{B} - \mathbf{A} = 0.64 \ m.y$
2	I_s, I_B and B	1865 (a)	$I_B - B = 218.27$,,
		(b)	$I_{s} - B = 86.81$,,
	4	(c)	$ _{B} - _{S} = 131.46$,,
3	$ _{S}, _{B}$ and A	1867 (d)	$I_s - A = 80.84$ "
		(e)	$I_B - A = 212.64$,,
		(f)	$I_B - I_S = 132.06$ "
4	I_s and A	1870	$l_s - A = 84.03$ "

By combining results (c) of comparison No. 2 with (e) of comparison No. 3, a value of $I_s - A$ is derived, viz. $81 \cdot 18 \ m.y$. Again, combining this value with result (d) of comparison No. 3 and the result of No. 4 comparison, and giving double weight to the latter, we get as a mean value

$$\mathbf{I}_{S} - \mathbf{A} = 82 \cdot 52 \, m.y.$$

Combining this with Clarke's value of $I_B - I_S$, + 131.46 m.y., we get

$$I_R - A = 213.98 m.y.$$

In 1870 these were accepted as the most probable values of the differences of length of the three bars.

No further investigations were made until the end of 1907, when the comparisons to be now described, were undertaken. The causes that led to this enquiry have already been stated.

It was at first intended to carry out a complete determination of the coefficients of expansion as well as of the relative lengths of the bars. With this object in view, suitable apparatus was designed. In consequence, however, of the necessary observers having to be obtained from field parties, the normal work of which would be temporarily suspended, the investigation of the expansions which would take a considerable time if results of any value were to be obtained, was abandoned, and the available means devoted to a careful comparison of the relative lengths at temperatures differing but little from 62° F.

The observations were commenced on 21st November, 1907, and were finished on 11th January, 1908, the observers being Major G. P. Lenox Conyngham, R.E., Captain H. M. Cowie, R.E. and Mr. J. de Graaff Hunter, M.A.

Of the difference $I_s - A$, 42 determinations were made, the temperatures during the observations ranging from 56°.5 to 68°.9. Of the two bars I_B and A, 38 comparisons were carried out at temperatures varying from 55°.5 to 69°.2.

The final results of the observations were

$$I_{s} - A = 83.12 \text{ m.y at } 62^{\circ}$$

the mean temperature during comparison being 61° 15,

and $I_B - A = 196.73 \text{ m.y}$ at 62°

the mean temperature during comparison being 61°.38.

The details of these observations are given later. On the conclusion of these investigations, bar **A** was sent to Sévres for comparison with the International Metre; after which it was once more returned to Dehra Dūn.

On its receipt there, the second series of comparisons was made. This was commenced on 17th November and concluded on 1st December, 1908, the observers being Captains H. H. Turner, R.E. and H. M. Cowie, R.E. Twenty sets of comparisons were made of each bar I_B and I_S with **A**. In the case of the observations of $I_S - A$, the temperatures ranged from $61^{\circ} \cdot 1$ to $65^{\circ} \cdot 0$ and during the comparisons of I_B and **A**, they varied from $57^{\circ} \cdot 0$ to $65^{\circ} \cdot 5$.

The results obtained were

$$I_s - A = 81.13 \ m.y \ at \ 62^{\circ}$$

the mean temperature being 63°.74,

and
$$\int_{B} - A = 193.38 \ m.y \ at \ 62^{\circ}$$

the mean temperature during observations being 61°.99.

A comparison of these two sets of values will at once show that it is probable no change took place in the length of the Standard Bar A between the time it left Dehra and the date of its return from Sévres.

In the reduction of the observations, the absolute expansions used were those adopted in 1870, viz.,

Expansion of
$$A = 21 \cdot 797 \ m.y$$
 for 1° F.
 $I_s = 21 \cdot 225 \ , \ , \ ,$

The comparisons were carried out in the Bar Room at Dehra. This room has three outer walls, along one of which runs a verandah. It is double rooted, the inner flat roof being of concrete, the outer sloping one of corrugated iron. To protect the building from the sun's direct rays, two outer walls and the roof were first covered with thick thatching and then outside this, leaving an air space of some 4 feet, were erected thick thatch walls, enclosing the whole building. Provision was also made to prevent the ingress of air from the outside when the observers and recorder entered the room. Two small glazed openings were left in the thatch walls to admit sufficient light to illuminate the defining marks of the bars when these were brought under the microscopes.

Within the room, the comparing microscopes, G and H, were placed on isolated brick pillars, east and west of one another. Between the pillars a travelling platform 8 feet 3 inches long and 4 feet 3 inches wide, was mounted on rails and capable of movement from north to south. On this platform were supported the bars and the bar boxes, the former on camels, the latter on wooden blocks as their weight and design made it impracticable to place them on the camels.

On account of the dimensions of bar A differing slightly from those of bars I_{R} and I_{S} , the box for the former was not exactly the same size as the box for the latter. The box consisted of two parts, an inner U shaped, double walled tank of

galvanized iron fitting in an outer wooden case, the space between the two being packed with coarse felt and wool. The hollow U tank had been intended for the expansion experiments which were afterwards abandoned. In this investigation it had been proposed to bring the bar under consideration to any required temperature by means of hot or cold water admitted into this tank. Through the bottom of the tank were openings to admit the blocks carrying the rollers on which the bar rested. The interstices between these blocks and the tank were filled loosely with felt. Each box was provided with four thermometers one at each end dipping into the interior of the tank, to indicate the temperature of the water, and two more in the central channel in which the bar was disposed. These thermometers, passing through holes in the top of the tank and kept in position by felt wads, had to be withdrawn to be read.

Each bar in addition was provided with two bent bulb thermometers, the bulbs of which were placed in wells in the bar, filled with mercury or oil according to the nature of the bar. These thermometers were viewed through glazed openings covered by a felt flap removable at will, in the top of the tank and box.

The bar and its enclosing box each had its own supports. The box was supported on the travelling platform by four pairs of wooden blocks, cut to a suitable height to allow the bar, when adjusted with its defining marks in focus under the microscopes, to lie centrally in the inner channel of the tank.

The bar itself was carried by its rollers at the usual points of support. These rollers were mounted on wooden blocks, which passing through the openings in the tank and wooden case, were fixed to the longitudinal beam, which, in turn, rested on two camels. The openings in the box were of such a size as to allow of a small amount of traversing of the blocks carrying the rollers. This traversing was effected by means of the adjusting screws of the camels which acted directly on the longitudinal beam.

The two bars under comparison were arranged in their respective boxes, side by side on the traveller, by moving which each bar could be brought in turn under the microscopes. The defining marks at the ends of the bars were brought into focus in the usual way by means of the camel screws. It may be remarked here that an adjustment once made was maintained by the bars for a considerable time, and it was found that the movement of the traveller did not cause any disturbance of the focal adjustment.

In the top of the iron tank was an opening over each defining mark of the bar, to allow of the latter being viewed in the microscope. These openings could be covered when observations were not in progress by felt and a flap, hinged to the cover of the wooden case. The thermometers used in the comparisons were :--

Bar	A.
-----	----

In	the bar,	east end		β
	>	west "		a
In	the central ch	annel, east "	Hicks,	379900
	••	west "	,,	361379
In	the tank,	east "	,,	no number
	,,	west ,,	,,	,,

Bars I_B and I_{S} .

In	the bar,	east end	Casella,	7349
	"	west "	,,	7344
In	the central channel,	east "	Hicks,	719477
	"	west "	Casella,	11923
In	the tank,	east "	Hicks,	No. 8
	,,	west "	,,	no number

Between 14th and 22nd November, 1907, these thermometers and others were compared with the Standards Nos. 105368 and 105369 at temperatures ranging from 33° to 100° F. During the comparisons all the thermometers were wholly immersed in water in a glass tank. The water was brought to the required temperature by the introduction of either ice or hot water and thoroughly agitated to dispel irregularities of temperature. The readings were made by means of a telescope.

The corrections to thermometers 7344, 7349, 719477, 11923, 379900, 361379, No. 8, a and β as tabulated in Table I were deduced from the observations, and are based on the assumption that the mean corrected reading of the two standards indicated the true temperature.

TABLE I.—Corrections to Thermometers.

Indiastud	Thermometer number								
Temperature	7344	7349	719477	11923	379900	361379	No. 8	a	₿
	•	•	٥	0	0	• •	3	°	o
33 34	-1.10	-1.05					•••	+0 ₃ 0	-1.00
35								,,	**
36	"	"						••	,,
37 38	-1.15	"	-0'75	-0.22	-0.20	-0.20	-0.32	+0.25	"
39	12	"	"	,,	,,		,,	,, ,,	
40		<u> </u>					-0.30	<u>+0 20</u>	<u>"</u>
42	,, ,,	,,	••		,, ,,		0	+0'15	"
43 44	"	"		-o.eo	-0.65	**	-0.50	+0.10	-1.02
45	-1.10	,,	,, ,,	»» »			,,		
46	•1	,,	**	"	,,		,,	+0.05	,, ,
47 48	-1.12	• ,,	"	-0.02	13	, ,, ,,	· · ·		-1.10
49	"		"	-0.70	"		"	0.00	,,
50		-1.10			-0:50		-0:15	- 0:05	<u> </u>
52	,,	13 13	31 J1	-0.75	,,	"		"	
53	"	,,, ,,	11		,, - 0, 77	-0.25	"	-0.10	"
55	,, ,,	-105		- o``80	-0.80	-0.25	», ,,	.,	,
50	,,	,,	.,,	,,		,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,	,,	-0.12	,,
57 58	"	"	"	-0 [.] 85	-0.85	, ,, ,,	"	-0.50	-1.02
59		,,	,,	- ~ 3	-0.00		.,		
60		·	''	<u> </u>	-0:05	,	· "	,	
62	, » ,	- 1.00	~0'80	,,	-0.95	" "	**	,,	, ,,
ΰ3 64	"	"		-0.00	- 1,00	.,	•,	•,•	-1.05
65	,, ,,	"	_0·85	.,	,,	·· ·		- 0. 25	-0.95
66	,,	,,	,,	,,	"	17	,,	"	,
68	,,	-1.05	,,	"	-1.05	"		"	,,
69 70	,,		,,	,,	, ,,	,,,		"	,,
70			`						<u>''</u>
72	1, 1,	,,	,,	,, ,,	,,	-0.50	,,	, v , v	,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,
73 74	-1	.,	,,	"	- 0. or	· · ·	,,	"	-0.02
75	.,	,	,,	, " , `	-0.95	11	,, ,,	- 0, 35	- 1.00
76	"	1)	**	,,	,,	,,	-0.02		-1.10
77	-1.15	" 	,,	"	.,	,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,	"	,, ,,	
79 80	,,	.,	,.		,,	,,	,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,	-0.30	-1-15
81									
82	,,	,,	,,	"	**	•,	,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,	,,	-1.15
83	"	"	"	"	,,	17	"	-0.25	-1.10
85		,,	,,	"	"	,,		-0.40	- 1.05
86 87	,,	,,	"	,,	,,	''	"	-0.42	,,
88	н 11	,,	,, ,,	-0.02		"		"	
89 90	"	"	"		11	-0.25	10	,,,	,,
91		·	· <u>·</u> ···	·		<u> </u>			
92	,,		, " ,,					, ,, ,,	
94 94	-1.20	~1.10	-0:00		- 1.00	-0.30	"	**	-1.12
95		-1.15			,"	,,		-0.20	
96 97	33		,,	,,	,,	,,	"	"	
96	"	-1.20	, " ,,	-0.00	-1.05	-0.32	, v	-0.22	**
99 100	0	- 1 . 00		, "´	, » [°]			-0.60	,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,
L	,,] "	-0.02	ļ ''	ļ »	, v	, "		, ,,

The values of the micrometer screws of G and H microscopes were determined between the 21st and 29th November, 1907, by measuring, in terms of these screws, the spaces between the dots $3 \cdot 0$ and $3 \cdot 5$; $3 \cdot 5$ and $4 \cdot 0$; $7 \cdot 5$ and $8 \cdot 0$; $9 \cdot 0$ and $9 \cdot 5$ of the inch "a b" of the steel Foot 1F, the value of all these spaces being accurately known. To indicate the temperature of 1F, thermometer No. 4246 was fitted to the bar, its bent bulb projecting into a well, filled with mercury.

The bar itself was supported by a short iron girder resting on two camels, by means of the screws of which girder and bar could be moved in any desired direction.

Six sets of observations were made with each microscope, the observers being Major G. P. Lenox Conyngham, R. E., Captain H. M. Cowie, R. E. and Mr. J. de Graaff Hunter, M.A.

The values of the sub-divisions of the inch "a b," determined in 1870-71 are recorded in Appendix No. 9 of Vol. I of the Account of the Operations of the Great Trigonometrical Survey of India. These values were adopted for the purposes of the present investigation. For the spaces observed they are

	<i>m.y</i>
Space	3.0 to $3.5 = 1385.573$
,,	3.5 to $4.0 = 1388.853$
1,	$7 \cdot 5$ to $8 \cdot 0 = 1388 \cdot 913$
,,	$9 \cdot 0$ to $9 \cdot 5 = 1391 \cdot 323$.

The coefficient of expansion of $|\mathbf{F}|$ was taken to be 0.000006367, the same as that of the steel bar $|_{\mathcal{S}}$ (vide p. (19), Vol. I).

The observations and the results obtained are summarized in Tables II and III.

TABLE II.—Determination of Micrometer Value of G Microscope.

Set	Dute	Observer	Space of inch "a b"	Mean observed value of space in terms of G	Mean Temperature	Reduced value of 1 aiv. of G in m. y
1	1907 Nov. 21	Н. М. С.	3.0-3.2	divisions 1202°54	68 [°] 56	1,1223
			3.5-1.0	1206.82	68 . 14	1.1209
			7·5-8·0	1205.62	68 ' 30	1 * 1 5 2 1
			9.0-9.2	1208.50	68.14	1.1213
					Mcan	1.1516
2	Nov. 21	н. м. с.	3.0-3.2	1203.08	67.21	1.1212
			3.2-4.0	1205.28	67 47	1 ' 1 5 2 3
			7.5-8.0	1205.94	67.79	1.1218
			9.0-9.5	1 208 . 62	68.02	1.1212
					Mean	1.1212
3	Nov. 22	G. P. L. C.	3.0-3.2	1200.34	67.09	1.1544
			3.2-4.0	1206.20	67.16	1 ' 1 5 1 2
			7.2-8.0	1213'12	67 · 23	1.1242
			9.0-9.2	1207.70	67.27	1 1 1 5 2 1
					Mean	1.1231
4	Nov. 22	G. P. L. C.	3.0-3.2	1202.22	67.75	1.1220
			3.2-4.0	1204.32	67.60	1 * 1 5 3 3
			7·5-8·0	1 204 . 58	67.85	1.1231
			9.0-9.2	1207 . 72	67.93	1.1221
					Mean	1 * 1 5 2 8
б	Nov. 23	J. de G. H.	3.0-3.2	1201.20	67.16	1.1230
1			3.2-4.0	1 203.90	67.04	1.1537
			7.2-8.0	1 205 ' 4 2	66 · 90	1 • 1 5 2 3
			9.0-9.2	1 208 . 98	66.75	1 . 1 509
					Мевл	1 . 1 5 2 5
6	Nov. 23	J. de G. H.	3.0-3.2	1201.94	67.25	1.1528
			3.2-4.0	1204 . 22	67 · 20	1.1534
	ļ		7.2-8.0	1204'76	67.14	1.1229
			9'0-9.5	\$ 207.72	67.06	1.1221
					Mcan	1.128
	F	inal value of :	1 division of	G = 1.15241	m. y.	

TABLE III .-- Determination of Micrometer Value of H Microscope.

Set	Date	Observer	Space of inch "a b"	Mean observed value of space in terms of H	Mean Temperature	Reduced value of 1 div. of H in m. y			
1	1907 Nov. 25	H. M. C.	3'0-3';	divisions	66° · 20	1.1000			
-			3.2-4.0	1256.28	66' 25	1.1020			
			7.5-8.0	1256.10	66.21	1'1057			
			9.0-0.2	1250'36	66.66	1.1048			
					Meau	1.1024			
2	Nov. 25	G. P. L. C.	3.0-3.2	1252.60	66.94	1.1062			
			3.2-4.0	1254.26	66.84	1.1023			
			7.5-8.0	1254.62	66.71	1.1071			
			9.0-9.2	1256.78	66 . 53	1.1021			
					Mean	1.1069			
3	Nov. 25	J. de G. H.	3.0-3.2	1 2 5 2 ' 80	67.60	1.1000			
			3.2-4.0	1 2 5 5 * 2 6	67.54	1.1062			
			7.2-8.0	1256.52	67.44	1.1024			
			9.0-9.2	1259.52	67:32	1.1042			
					Mean	1.1022			
4	Nov. 26	Н. М. С.	3.0-3.2	1253.64	65.66	1.1023			
			3.2-4.0	1257.32	65.99	1.1040			
	1		7.5-8.0	1256.82	66 - 29	1.1021			
			9.0-9.2	1260'42	66 · 50	1.1030			
					Mean	1.1042			
5	Nov. 26	J. de G. H.	3.0-3.2	1252.94	67.35	1,1020			
			3.2-4.0	1255.12	67 . 23	1.1066			
			7.2-8.0	1255 64	67.01	1,1003			
			9.0-9.2	1259.50	66 · 78	1.1042			
1					Mean	1.1020			
6	Nov. 28	G. P. L. C.	3.0-3.2	1255.16	66 - 57	1.1030			
l			3.2-4.0	1255.42	66.75	1.1063			
			7.2-8.0	1255.74	66.88	1.1001			
			9.0-9.2	1257.88	67.00	1.1001			
		l		1	Mean	1.1026			
Final value of 1 division of $H = 1.10570 m. y$. Hence, 1 division of $H = 0.95947$ division of G.									

The errors of the thermometers and the micrometer values of the two microscopes having been determined, the comparisons of the bars were commenced.

The procedure of the observations was as follows:-On the traveller were disposed the two bars, A and either I_s or I_p , carefully adjusted in position and levelled. One bar was then brought under the microscopes, which were then adjusted correctly over the defining marks, levelled and set so that the images of the marks were in sharp focus. The mounting of these microscopes is very stable and throughout the operations there arose no reason to suspect any change of setting or position. The two microscopes, thus adjusted, constituted the comparator and from this point onwards, the lengths of the bars were referred to the distance between the zeros of the microscopes, which quantity was necessarily assumed to remain constant. This assumption is justifiable, as the interval of time between the measurement of one bar and the measurement of the other to be compared with it is very small. At each microscope was an observer, who also took readings of one of the two thermometers giving the temperature inside the tank, one of the two thermometers in the central channel and one of the two bar thermometers. The eastern observer, in addition, read the thermometer giving the temperature in the room.

To illuminate the scales of the thermometers and the drums of the micro meter, small electric glow lamps were used.

The following is the programme of the observations of one set; bar I_s , let us say, being under comparison.

Bar A was brought under the microscopes and examination was made of the quality of the focal setting of the defining marks. The same was then done for I_s .

The focal setting and positions of the bars having been examined and corrected if necessary, the eastern observer read the thermometer giving the room temperature. Then followed in order

(1)	The reading	s of t	he tank thermometers,)
(2)	,,	,,	central channel thermometers,	ſ
(3)	,,	,,	bar thermometers,	1
(4)	,,	,,	microscopes G and H,	For bar I.
(5)	,,	,,	bar thermometers; after which the	
			traveller was moved till bar A came	
			in position.	j

(6)	The readings	of the	e bar thermometers,	h
(7)	,,	,,	microscopes G and H,	
(8)	,,	,,	bar thermometers,	
(9)	,,	,,	central channel thermometers,	
(10)	,,	,,	tank thermometers,	Ton bon A
(11)	,,	,,	bar thermometers,	For bar A
(12)	,,	,,	microscopes G and H,	
(13)	,,	,,	bar thermometers; after which the	
			bar $ _{s}$ was again moved under the	
			ر microscopes.	1
(14)	The readings	of the	e bar thermometers,	1
(15)	,,	,,	microscopes G and H,	
(16)	,,	,,	bar thermometers,	
(17)	,,	,,	central channel thermometers,	For bar I_s
(18)	,,	,,	tank thermometers; after which the	
			room thermometer was again read	ļ
			by the eastern observer.)

This constituted one set of observations. The observers then changed places and a similar set was taken.

Each day two sets were observed while the temperature of the outer air was rising and two while it was falling. At each observation with the microscope at least three intersections of the defining mark were made. The intersections of the east and west marks were made simultaneously and no readings were taken unless both observers were satisfied that their respective intersections were good. In all observations whether with the microscopes or the thermometers, the eastern observer made his reading first.

During sets Nos. 1-10, 22-32, the heads of the micrometers were turned towards one another and in the remaining sets, away from one another. In the former case, increasing micrometer readings corresponded with an increasing length of the bar. Thus if D represents the distance between the zeros of the microscopes, L the length of the bar and M the sum of the micrometer readings,

$$\mathbf{L} = \mathbf{D} + \mathbf{M}.$$

In the latter case, where the micrometer heads were turned away from each other, increasing readings corresponded with a decreasing length of the bar. Hence, L = D - M.

On the 31st December, to maintain the temperature at the required point, two small stoves were placed in the room and kept at a low heat. On the 4th January two more stoves were introduced.

Table IV is an abstract of the observations and shows the resulting values of $I_s - A$: and Table V gives the same information with respect to the bar I_B . The values of $I_s - A$ and $I_B - A$ together with the mean temperature of the bars compared are summarized in Table VI.

In all cases G microscope was at the east end and H microscope at the west end.

TABLE IV - Abstract of Comparisons between A and Is with deduced results. (Micrometer heads turned towards each other).

$I_S - A$	at 62° F.	19.28	11.88	83.20	91.61	96.88	17.88	50.98	82.73	8o 84	83.36	t6.95	11.08	85.95	
Reduction to	62° F.		+ 76°52 + 76°53	01.98 + 06.22 +	+ 77.68 + 87.62	+ 75°77 + 75°57 +	+8.62 + 12.42 +	+ 90.68 + 90.68	+ 83.84 + 92.64	+ 82.35 + 89.37		29.611 + 62.011 +	+ 109° 10 + 113• 56	+ 108°67 + 112°69	
ed values of d A - D	in <i>m.y</i>	1892.70 1808.36	1893 74 1810 52	1888-05 1796-65	1888 go 1799 20	01.2081 1801.37	1896 18 1896 18	1880°98 1787°24	1790-99	22.9621 80.1881	1888 · 67 1800 · 08	1847°20 1761°38	1851.95 1767-38	1766 - 87 1766 - 90	m.y F
Mean observ I _S – D an	in terms of G	02.6951 82.2791 82.2791	20.1251 62.8791	to.6251 1638.35	1561 25	1263.77 1563.77	29.4951 04.5491	1550'87	1633+55 1554*13	99-8231 06.1291	1638°89 1562°02	1602°90 1528°43	tg.2231	1533.22	82.85 57°.86
, ean	Bur	58.26 58.28 58.28	58 39 58 48	58 33 58 05	58°34 57°98	58.43 58.28	58-48 58-36	58 00 57 84	50.85	58.12	58 - 19 58 - 05	56-78 56-78	56°79	56-88 56-83	other)
orrected temperat	Air space	\$8.50 58.98 58.98	58'93 59'33	58°25 58°23	58.35 58.38	58.63	58 73 58 73	60.85	58.23	58°35 58°33	58.29	57.03 57.03	57 18 57 05	57.20	ls each o
Uean U	Room	59.65	59°80	58,78	\$0.65	81.65	59.65	58 63	54.85	20.25	\$4.65	01.15	06.15	58.20	ed toward
P		-~<	_°<	_°^ <	_ ₂₂ <	_ _∞ ∢	- ^s 4	-~~ <	_s.<	_∞ ∢	- <u>s</u> ×	_v. <	<u>~</u> ∾∢	_°. <	ads turne
bservers	West end	J de G. H.	Н. М. С.	Н. М. С.	J. de G. H.	J. de G. H.	Н. М. С	Н. М. С.	J. de G. H.	J. de G. H.	н. м. с.	H. M. C.	Н. М. С.	G. P. L. C.	(micrometer he
Position of o	East end	H. M. C,	J. de G. H.	J. de G. H.	H. M. C.	H. M. C.	J, de G. H.	J. de G. H.	Н. М. С.	Н. М. С.	J. de G. H.	G. P. L. C.	G. P. L. C.	Н. М. С.	еап value of 1 _S — А ean temperature
	e	1	16	17	17	17	11	8	18	18	81	24	54	24	MM
-	1.041	190 Dec.	•	2	2	÷	÷	2	2	2	=	:	=	ŗ	
No. of	set.	-	8	en	-7	10	<u>د</u>	r-	or)	G	10	53	23	24	

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ls − A ot	G2° F.	m.y 86 · 60	88 . 50	80.46	85.59	37.58	82.85	85.21	84.25	89.74	84.21	87.24		8,3 92	78.85
Reduction to	62′ F.	- 97.21 - 97.21	- 88.93 - 98.74	- 86°81 - 94°38	- 85'96 - 85'96	+3.801 - 60.96 -	61.to1- 88.t6 -	12.26 -	- 92 97 - 97 43	- 113.78	09.111 - 92.901 -	- 110.37		+ 43.72 + 39.45	+ 43.51 + 40.54
ed values of nd 1) – A	in <i>m.y</i>	26.951 2751-37	2656°55 2754°86	2656-65 2744-68	5712.04 2712.90	2665°11 2757°31	2666-85 2759-01	2661 . 77 2750 · 80	2662 37 2751 08	2678-27 2773-54	2677+74 2766-79	2682 96 2780 80		2209'29 2209'29	20.2622
Meun observ U = U _S u	in terms of G	dirus. 2305 53 2387 49	2305 21 2390 52	69.1882 2302.30	2300°66 2379°40	2312°64 2392°65	2314.15 2394.12	2309.74 2387.00	2310.26 2387.24	2,324°06 2,324°06	2,323 60 2,400 87	2328-13 2328-13		89.8661 01-2161	92.6861
tures	Bur	° 57:79 57:54	57.81	29.23	57.95	57.52	57.53	57.60	57.53	56.78 56.78	26.95 26.95	56.80 56.45		18.E9 63.81	64 °05 63 °86
Jorrected temperat	Air space	\$7.77 57.77 57.80	58°02 58°00	58°08 58°25	58.23 58.23	57'48 57'40	57-82	57 65 57 65	58°03 57°80	57.15	57.30	56.93 56.70		64 · 03	64.08 64.08
Mean	Room	58.50	58.65	o.'.83	01.65	58.15	58.35	01.82	56.85	82.15	58 ° 08	07.15		65.70	65.85
		_ <u>s</u> <	_°.∢	-° <	- <u>s</u>	-° <	_°. <	P. A	<	- <u></u> ~ <	~s ×	- <u>s</u> 4		_ _S	_ ₈ 4
f observers	West end	И. М. С.	J. de G. H.	J. de G. H.	Н. М. С.	Н. М, С.	J. de G. H.	Н. М. С.	J. do G. H.	G. P. L. C.	H. M. C.	G. P. L. C.		G. P. L. C.	Н. М. С.
Position o	East end	J. de G. H.	H. M. C.	Н. М. С.	J. de G. H.	J. de G. H.	н. м. с.	J. de G. H.	Н. М. С.	Н. М. С.	G. P. L. C.	н. м. с.		Н. М. С.	G. P. L. C.
		10	19	19	19	20	20	20	20	23	23	24		4	4
	Date	1907 Dec.	=	=	£	, :	-	:	£	2	2	÷	1908	Jan.	÷
No of	ect.	=	13	13	1	15	16	17	18	61	20	21		23	54

THE BAR COMPARISONS

TABLE IV.—Abstract of Comparisons between **A** and **I**_s with deduced results—(Contd.) (Micrometer heads turned analy from one another).

61.82 7.3.88 79.48 98.48 86.58 24.08 84-18 25.48 87.18 12.28 61.28 82.74 11.54 < 81.63 62° F. m, y T at 5 Reduction to 62 F. *m.y* 63.89 64.96 62.37 61.69 +6.65 89.69 99.99 97.69 71.95 71.28 69.62 65.83 +139.45 + 145 39 68-98 63-87 65 37 63 21 26.6j 8.4 tz.9t1 + + 147.57 + 146-88 60.671+ ÷ + + + + ŧ + + + + + + + + + + + + 4 + 2157°83 2157°83 09.6922 88.1612 2074 82 2152 72 2159.48 2237.15 2157.63 2241.41 Mean observed values of 11.1222 2135'30 15.6222 12.9185 2327.10 2165.80 10. ++22 3.2 26 26 29.1072 29.01:2 m.y $D - I_S$ and D - A2385 2313 Ξ. in terms of G 2009 - 88 2084 - 00 1902 00 1969 44 1852.90 1873-88 1945-60 1879.37 18. t902 2070'10 2070'38 60 82 20191233 1872.45 1872.45 1872.28 1970.75 1800.42 81.140 2019-42 dirns. 2007 68.89 68.89 64 63 65 25 65 · 18 64 · 82 65 °08 64 °90 65°08 64°83 65.00 65.00 82.tg 65°01 65°01 65°28 65°02 24 65°32 65°21 65 39 65 27 33 8⁴ Bar . 89 98 Mean temperatures <u>8</u>83 Corrected Air space 9. 8. 8. 8. 66.13 65.93 65.08 64.88 65.08 65.08 65.10 65.10 65 33 64 98 65°10 65°08 65.58 65.68 65 · 65 65 · 83 30 95 95 83 **08** 95 8 8 . وزوره . 89 ŝŝ ંજી 50 69 51.69 70.25 01.69 65.75 o£.99 66.45 99.45 01.19 8 ŝ 59.99 8 Room S 5 °.6 . 69 2 <u>6</u> <u>.</u>89 Bar **-** • - s • - × --<u>s</u> 4 <u>~</u> < <u>~</u> < _∾ < <u>~</u>~∢ -^s < -° < ~~ < <u>~</u> < *"*∢ -~× G. P. L. C. J. de G. H. J. de G. H. G. P. L. C. G. P. L. C. G. P. L. C. J. de G. H. M. C. West end сj M. C. Ħ ් Ö Ċ H. M. М. М. H. M. J. de G. H Position of observers H. Ξ. Ħ J. de G. H. J. de G. H. Ħ, Ċ G. P. L. C. G. P. L. C. ပ East end H. M. C. J. de G. H. H. M. C. Ċ H. M. C. H. M. C. ບ່ P. L. P. L. J, de G H. M. Н. М. с. cj 10 ŝ 10 10 c e φ ω 1-5 5 r-Date 1908 Jan. = 2 = . : 2 : : \$ • 2 -2 No. of set 55 55 58 55 60 $\mathbf{62}$ 57 61 63 64 55 99 68 5

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(Contd.	
with deduced results.	from one another).
<u>~</u>	hpa
and	еф ан
2 A	11.19
between	heads to
Comparisons	(Micrometer)
of	Ū
TABLE IVAbstract	

, , , ,		Position o	f observers		Mean (Jorrected temperati	Ires	Mean observ D — 1 ₅ ar	ed mines of id D - A	Reduction to	ده ۱۳۳
N.	Date	East end	West end		Room	Air space	Har	in terms of G	in m.y	62 F	62° F
	1908				•		•	diens.		ų.m	н.у
63	Jan. B	J. de G. H	Н. М. С.	_» «	67.35	66 · 05 65 · 95	65,82 65,67	99.5861 99.5861	2284.49	66.62 +	69.7H
70	æ :	Н. М. С.	J. de G. H.	_° <	08.29	65 98 65 98	65 - 86 65 - 59	1909 55 57 2801	26.1822 2200.58	+ 81.93 + 78.25	80.66
											Ī

83.23 *m.y* 62°.63 F. Mean value of $l_s - A$ (micrometer heads turned away from one another) Mean temperature

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THE BAR COMPARISONS

TABLE V.—Abstract of Comparisons between **A** and I_B with deduced results.

(Micrometer heads turned towards each other).

v .	аг 62° F.		ħ.m	30.861	og. £61	15.661	200,00	91-861	20.261	o6.g61	81.861	
Reduction to	62° F.		m.y + 198.85	12.271 +	+ 199 17	+ 198 85 + 136 45	+ 198 19 + 135 58	+ 202.12 + 202.12	+ 201.47	+ 301.47	+ 198-85 + 135-14	
ed values of d = D	in <i>m.y</i>		1874.33	1732.36	187218 173522	1873.59	1877.76	1732-99	1870-88 1732173	1874°15 1743°32	1876 91 1742 44	7.00 m.y
Meun observ 1 ₁₀ – D an	n terms of G		divns. 1626 - 44	1503.25	1624-58 1505-74	1625 80 1511 98	1510-20	1 623°00 1 503°80	1503.57	1512.76 1526.29	1628 68 1512 00	51
67.IN	Bar		°, 55	55.45	55.92 55.47	55 93 55 74	55.95 55.78	55 83 55 53	55.85 55.46	55.85 55.79	55 '93 55 '80	i other)
Corrected temperat	Air space		56 o.3	55°7 ^B	55.78	56°23 56°30	56-20 56-20	55.98 55.78	56°18 56°18	56.15 56.38	56 · 28 56 · 28	trds each
Mcan	Room		56.50		26.70	57.15	ot.19	56.40	56.60	56.95	57.25	ued towa
Bar	1		- ⁸	<	- ^R 4	_ ^{RI} <	_¤<	BA	_ª<	_ ^{rq} <	_₽₹	eads turi
observers	West end		G. P. L. C.		H. M. C.	H.M.C.	G. P. L. C.	Н. М. С.	J. de G. H.	H. M. C.	Н. М. С.	— A (micrometer h
Position of	East end		Н. М. С.		G. P. L. C.	G. P. L. C.	Н. М. С.	J. de G. II.	Н, М. С.	J. de G. H.	J. de G. H.	Mean value of 1 _B Mean temperature
·`			26	_	20	26	26	22	72	22	27	
Date		1901	Dec.		2	÷	-	:	2	-	2	
No. of	1) 05 0		25	_	56	27	82	63	30	 18	55 57	

OF 1907 AND 1908.

197.00 *m.y* 55°.76 F.

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td.)	
(Con	
and] _B with deduced results—(t away from one another).
Ň	nec
F Comparisons between	(Micrometer heads tur)
9	
BLE VAbstract	
T.A.	

₁₈ - A	62• F.	т.у 200`40	£8.202	61.102	81.661	80. <i>1</i> 61	200' 15	£8.361	96.202		81.361	61.761	to .861	06.161	at.26:
Reduction to	62° F.	m.y 	28.181 - - 1991 -	- 198 · 19 - 134 · 27	- 197 21 - 134 45	- 198°52 - 138°19	- 198-85 - 138-85	- 198 85 - 134 71	- 198.52 - 13471		- 9.83 - 13.08	- 4·59 - 7·41	+ 4.26 - 1.09	+ + 5 .90 4 - 4	+ 30.47 + 15.04
ed values of a d	in m.y	2661 - 74 2800 - 40	2660 · 26 2801 · 24	2658 + 48 2795 * 75	2658 62 2795°04	2663 · 7.3 2800 · 48	2661 - 70 2801 - 85	2662 · 40 2794 · 09	2658'73 2797'88		2123.39 06.2252	2114'13 2314'14	2115-14	2113°64 2307°30	2077 • 53 2285 · 36
Mean observ I) — I _B ar	in terms of G	dirme. 2309°72	2308°43 2308°43 2430°77	2,306.89 2,306.89	10.22tz	2311-44 2430-11	2,309°68 2,309°68	2310°29 2424-56	2307 · 10 2427 · 85		1843°06 2015°25	1834°53 2008°09	1835.41 2007:56	1834 • 10 2002 • 15	1802.77 1983.11
tures	Bar	55.97	55-70 55-70	55.84 55.84	55.98 55.85	55-94 53-66	55.93 55.63	55.93 55.82	55 '94 55 '82	-	07.19 02.19	99 - 19 98 - 19	62.13 61.95	62°18 62°19	62 · 93
Corrected temperat	Air space	56°05	56.18 55.98	56°15 56°15	56.23	56.08 55.78	56.15	56°23 56°30	56.38	-	02.19 00.29	62°10 62°13	62.58 62.78	62.80 62.88	62.93 62.83
Mear	Room	56.50	56.80	56.75	57.30	56.35	56.65	9£.95	27.10	-	63 · 60	64 [.] oo	et.30	51.19	£1.15
ء 		_~	< _≃<	_¤∢	_ª<	_ª <	_ ^{eq} <	_ ^{eq} v	_ ^{eq} <		A ⁸ 4	- ⁸ 4	_≞∢	_ ^{eq} <	_~~
observers	West end	J. de G. H.	д. Р. L. C .	G. P. L. C.	J. de G. H.	Н. М. С.	G. P. L. C.	Н. М. С.	G. P. L. C.		Н. М. С.	G. P. L. C.	G. P. L. C.	Н. М. С.	J. de G. H.
Position of	East end	G. P. L. C.	J. de G. H.	J. de G. H.	G. P. L. C.	G. P. L. C.	н. м. с	G. P. L. C.	Н. М. С.		G. P. L. C.	Н. М. С.	Н. М. С.	G. P. L. C.	G. P. L. C.
			~			67	50	29	29		-	-	1	1	e)
	Ð	28	56	ត	61					80					
	Date	1907 Dec. 28	3	ñ :		=	*	÷	=	1908	J _{bn.}	2	÷	=	:

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THE BAR COMPARISONS

TABLE \mathcal{V} .—Abstract of Comparisons between **A** and $|_{B}$ with deduced results—(Contd.). (Micrometer heads turned away from one another)

◄ 09.561 92.861 82.26 62.16 194-52 12.461 51.261 12.16 62° F. 02.361 106.22 9**?** 16.26 3 00.101 I at n.y .86 5 <u>~</u> Reduction to 62° F. + 229.64 + 148-22 + 206 7 1 + 133 18 m.y 29.48 16.57 60.281+ 88.902+ + 210 . 31 + 138 . 85 + 236.85 + 235 ° 21 + 29.61 32.10 12.02 60.22 37.71 37 · 05 + 211.62 **t6.6E1** + + 72°40 + 74.36 + + + + + + + + + + 2115.46 1322.04 14.7925 1960-45 2245°17 92.8812 98.2002 10,1022 09.6/61 77.6122 1997-86 2218-56 12.8182 28.8102 1953.47 i vulues of 1 D - A 2088.052 88.9622 2113.57 91.9612 26.9261 2050.66 16.4622 12.1602 2318-71 ∢ ų.m <u>, E</u> Mean observed v_1 D - 1_B and Γ terms of G 20.2102 1760°29 12.1861 62.8821 divns. 1811-88 1834.04 1835-68 2014-94 76.6061 1728.62 1733.64 1779.45 to.8941 00.1661 1936.45 tz . 8+61 19.4121 66.0261 695-12 11.5661 12.5001 Ë. 62.76 62.76 62.98 80.29 63.01 10.29 63.90 63.73 04.E9 06.E9 64 - 20 64 - 27 20.69 82.69 26.89 81.69 12.49 64 ' I I ~ = 8.8 31 46 28 Bar Corrected Mean temperatures 89.89 89 89.89 ંજું Air space 63°17 63°17 63°13 63°32 64°03 64°03 64.38 64.48 63.15 63.28 63.88 63.88 64°53 64°72 68.38 68.35 68 . 35 68 . 35 68.85 68.85 20.69 21.69 02.69 88.69 2 % ŝŝ . 38 09.12 50.59 50.6g 02.69 64-65 68 9.3 \$ 08.89 **0**8-69 20 73 35 Room 71.45 °;• <u>و</u>: <u>.</u> ġ ġ è Bar -^A4 _~~ < ~^{~~}< **_**^{₽q} **<** _A< _∾∢ <u>_</u>^m< <u>_</u>^m< <u>_</u>^m< <u>^</u>< _°°∢ _¤∢ _**P**∢ _∾< с, Ċ Ξ Ħ Ξ Ö v end с, Ö Η c) H. Ö G. P. L. C. G. P. L. G. P. L. J. de G. J. de (ì. P. L. J. de G. ц, J. de G. J, de G. 1 West 6 М. Я Ж M. e. Position of observers H Η щ щ Ċ Q, Ġ. P. L. C. Ħ D, J. de G. H. J. de G. H. Ħ, P. L. C. J. de G. H. J. de G. H. end H. M. C. сi Ħ H. M. C. Ö G. P. L. J. de G. J, de G. Н. М. ¢ H. M. East . de de đ Ŀ, 2 ¢1 ¢1 en: ŝ c a ŝ G o, S, 6 ្ព 10 2 Date 1908 Jan. 2 = : = 2 2 : \$: 2 2 = \$ No. of set 9 4 9 49 20 51 52 7 23 53 4 2 26 E

OF 1907 AND 1908.

TABLE V.—Abstract of Comparisons between **A** and I_B with deduced results—(Contd.). (Micrometer heads turned away from one another).

- 	E to B - A	. 62° F.	<i>¹</i>	31 196'14 B7 196'14	73 195°98	40 54 195°63	
	Reductio	62° F	<i>n</i> m	+ 148.1	+ 120.	+ 186	
	ved values of	in <i>m</i> .y		2006 - 30 2282 - 88	18.9/22 98.4102	2011-97 2273°46	96°65 <i>m.y</i> 62°-88 F.
	Mean observ U — 1 _B a	in terms of G	dinne	1740°96 1980°96	92.5261 26.2471	1745°88 1972+79	er) 1
	turee	Bar		69°00 68-83	67.70 67.54	67.53 67.53	ue anoth
	Corrected n tempera	Air space		69°08 68°95	68.00 67.70	68° 00 67° 90	from ot
	Mea	Room		06.ºL	o6.6g .	20.50	ied away
	۽ 	ла 		_a <	_~~	_ ^R <	eads turi
	of ubservers	West end		J. de G. H.	н. м. с.	J. de G. H.	– A (micrometer h
	Position (East end		G. P. L. C.	J. de G. H.	Н. М. С.	Mean value of 1 <i>n</i>
		9	8	01	11	=	
		Dut	100	Jun.	÷	:	
	- Ju v			78	ŝ	a	

THE BAR COMPARISONS

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Mean temperature

No. of set	Mean temperature of Bars Is and A	Value of 1 ₈ – A	No, of set	Mean temperature of Bars I _B and A	Value of $I_B - A$
		<i>m.y</i>			m.y
1	58.27	82'64	2D 90	55 09	102.80
2	58+44	83.11	∠ 0	5 70	193 00
3	58.19	83.20	21	55-83	+93 57
4	58.16	79.70	28	55-87	200.00
5	58.35	83.96	29	55.68	198.40
6	58.42	88141	30	55.62	197.07
7	57.97	86.02	31	55.82	196.90
8	57.90	82.73	32	55-87	198118
9	58.01	80-84	33	55.87	200.40
10	58.12	83-36	34	55.81	202.83
11	57-66	56÷60	35	55.89	201.19
12	57.64	88.20	36	55.92	199-18
13	57.79	80.40	37	55.80	197 08
14	57.89	85.59	58	55-78	200 ' 1 5
15	57:38	83.75	39	55-87	195-83
16	57 38	82.85	40	55-88	202-96
17	57 57	85.21	41	61.55	195-18
18	57.57	84.25	42	61.76	197.19
19	56.84	· 89'74	43	62.04	193.04
20	56.93	84'21	44	62-18	191.90
21	56.63	87-24	45	62,81	192.40
22	56-64	76-94	46	62-83	195.94
23	56.83	80.11	47	62-94	195-60
24	56-85	85.95	48	62.97	193.26
53	63.93	83.92	49	63-82	195.70
54	63 · 96	78.85	50	63.80	196 - 22
55	65.00	78.79	51	64.16	195.28
56	65-15	73.88	62	64 . 23	194 ' 29
57	68.52	79.48	71	68 • 2 1	194.22
58	68·78	84.86	72	68 18	195.55

TABLE VI.—Values of $I_S - A$ and $I_B - A$ reduced to 62° F. as determined at Dehra, Nov. 1907—Jan. 1908.

No. of set	Mean temperature of Bars I _S and A	Value of I _S - A	No. of set	Mean temperature of Bars I _B and A	Vulue of I _B - A
59	6×83	m y 83-98	73	6Å·40	<i>m y</i> 194'71
61	68-88	80 42	74	68.44	197+15
60	65.00	81-63	75	69 · 1 2	194.27
62	65.00	84 18	76	69.07	201.00
63	64.99	81.22	77	68 . 90	198+56
64	64.96	81-73	78	68.92	196-14
65	64.87	82 74	79	67.62	195.98
66	64.89	87.19	80	67.61	195-63
67	65 : 27	82.24			
68	65.33	83.11			
69	65.75	82.69			
70	65.72	80 · 66			

TABLE VI.—Values of $|_{s}$ – A and $|_{B}$ – A reduced to 62° F. as determined at Dehra, Nov. 1907 – Jan. 1908—(Contd.).

TABLE VII.—Mean values of $|_{s} - A$ and $|_{B} - A$ reduced to 62° F. from Dehra observations, Nov. 1907—Jan. 1908.

	I_S — A and Temperaturo	I_B — A and Temperature
Mean value for temperatures below 62°	83 98 m y	198 · 22 m.y
Corresponding mean tempera- ture	57 64 F	5 6 · 46 F.
Mean value for temperatures above 62°	81 97 m y	195·38 m.y
Corresponding mean tempera- ture	65 84 F.	65 [.] 81 ፑ.
General mean value General mean temperature	83 ·12 ± 0·33 m.y 61·15 F.	196·73 ± 0·30 m.y 61·38 F.

After these observations had been completed bar **A**, as stated above, was sent to Sévres for comparison with the International Metre. It was then returned to India, and a second set of comparisons was carried out in November and December, 1908. The same method and procedure in general was followed as had been done in the comparisons already described. No new determinations of the thermometer errors were made, but the same thermometers were used in identical places; nor were the values of the micrometer errors of G and H microscopes redetermined. The old values in both cases were accepted.

Comparisons Nos. 1 to 10 inclusive and Nos. 31 to 40 inclusive dealt with the differences $I_B - A$. Of these comparisons Nos. 1 to 10 were made with the micrometer heads turned towards each other and with the end of the bar **A** marked "Troughton and Simms" towards the west. In the remainder the heads of the micrometers were away from one another and "Troughton and Simms" towards the east. Comparisons Nos. 11 to 30 inclusive gave values of the quantity $I_S - A$. Of these Nos. 11 to 20 were made with the micrometer heads towards each other and "Troughton and Simms" towards the west. In the remaining comparisons these conditions were reversed. The two observers H. H. T. and H. M. C. as in the 1907 comparisons changed places, so that each day an even number of comparisons were made, half under one and half under the alternative conditions. At no time during the operations were stoves necessary for maintaining the temperature of the room at the required height.

The same particulars of these observations as have been given for the previous set, and their results are set forth in Tables VIII-XI.

TABLE *VIII.***—Abstract of Comparisons between A** and **I**_R with deduced results. (Micrometer heads turned towards each other).

• 61.96 **†1.96**1 88.66 92.261 62° F. 82.28 62.261 21.061 17-501 06.061 10.161 6.11 - " ut Reduction to 62° F. - 69: 50 - 112:69 - 112:69 - 76.07 - 104 '83 - 62 34 61 07 193 07 25 96 - 75.42 13 <u>و</u>ي 9 53 99.711-- 103 -- 103 - 112 - 64 53 52. 1.1 1.1 1.1 Mean observed values of I_B - D and A - D 1798-97 1570-79 61.6231 1821-87 1587-56 1829 34 18,32°22 1813-85 1589°20 1798-58 1570-27 10.2181 1579.35 18.128 11.11 5 in terms of G 580.92 377.60 587.40 1589-90 1389-26 1572.37 1573 96 1370 23 1376.63 12:00:71 1361.05 1363.05 1362-60 580.87 15.018 divns 65.42 64:98 65 • 44 65 50 65 46 65 • 48 65 • 49 65 20 64 86 65-15 64-85 65 16 63 06 64 : 85 64 : 56 18.49 64 · 52 64 · 52 17.79 Ваг Mean temperatures Air space Corrected 65.48 65.38 65.15 65.15 06.59 86.59 66.13 65.85 06.39 01.99 65 68 64 98 65.28 65.15 89.79 92.09 £7.49 06.49 65 °03 64 · 88 Room 99.10 65.85 65.35 و§ . 60 66-68 65.75 02.29 65.10 65.20 38 . 99 Bur _~∢ _^~< <u>~</u>< _^~< _^~< _∾∢ <u>~</u>< _°< _^A< _^e∢ West end ల H Ó ರ ei ÷ Fİ ರ Ċ H. H. T. H. M. Ä H Η̈́ Ä 넑 щ Ē Þ H. Position of observers Ë щ H. Ξ Ħ Ë Ħ сj ರ ల ల Ċ. East end ÷ ÷ Н. Т. H ÷ H. M. Ħ Ä N Ä Ħ H. Ä Ħ H. H. Ë Ë Ħ. нi Ħ Η. Ξ 8 90 9 6 61 5 5 11 17 61 Date 1908 Nov. = 2 2 = 2 2 2 ; : No. of set -61 ŝ ŝ ø ~ **6**0 თ ទ

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w.m. 72.291 ... 65°.05 F.

Mean value of $I_B - A$ (micrometer, heads turned towards each other)

Mean temperature

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TABLE VIII.—Abstract of Comparisons between **A** and 1_B with deduced results—(Contd.). Micrometer heads turned away from one another)

∢ 23.681 81.261 16.861 92.86 29.261 01.96 \$ 00.16 67.79 Ē 3 ų.m I B,t 3 . g .86 24 Reduction to 62° F. - 158 88 - 94-16 - 134'31 - 79'12 m.y 83.54 44°25 - 16.00 - 163-47 81.90 36.02 23.23 ÷; 55 88 28. 28. 8.8 . 63 ī I. 1 1 i 1 1.1 1.1 ī -i Mean observed values of $D = I_B$ and D = A57.000 10.247 7,38 · 42 892 · 33 713.78 02.296 29.9t6 9t.208 801°65 936°86 755°46 719.75 878-15 832''19 832''14 02 98 n.y 754. E. 5 29.182 291 (10 224.32 574.32 619.38 763.76 72213 83316 695.63 812.96 terms of 200.67 655°55 804°74 99 91 725.47 8.39.37 30 divns. 524 562 · 2.96. Ξ 59.45 59.97 50.09 05.65 60°58 60°58 69.09 †1.09 57.01 89.23 21.23 57.76 58.37 50.62 50.02 20.65 Bar Corrected Mean temperatures Airspace \$9.80 50.45 60.03 60.55 60.28 61.30 60 63 61 40 57°50 58°38 57.88 58.25 58.73 58 40 59 40 59.18 ő 4 . 62 £o.zg 62.40 Room 02.29 50.09 60.45 o£.og 75 59.65 \$6.65 2 . ق° .69 Bar -²⁹ • -^R < _^{eq} < _^{A9} < -[®] 4 _^A< _^A4 <u>-</u>~~ -^A < _^A< West end c, Ċ H. T. гi ÷ ö ÷ ບ່ U, Ŀ. Ä H. Ä Ħ Ä N. Ë. ਸ਼ਂ H Position of observers H Ħ Ħ Ħ H. щ H. н. Ξ Ħ East end ບ່ Ŀ ÷ Ċ, Ö ÷ н. Т. ບ່ U H H. M. (Н. М. Н. Н. н.н. Н. М. H.M. Ħ Н. М. H. H. Ä Ξ 27 53 51 5 30 8 30 30 -Date 1908 Nov. = 2 \$ 2 2 2 2 • Dec. No. of et 31 32 33 34 35 36 88 33 39 \$

OF 1907 AND 1908.

A (micrometer heads turned away from one another)

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Mean value of 1_B Mean temperature

194.50 m.y 58°.94 E.

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A and Is with deduced results.	towards each other).
TABLE IX.—Abstract of Comparisons between	(Micrometer heads turned

s - A	62° F.	1 60	98-18	83.56	81.82	80.59	80.32	78.42	20.28	11.62	85 . 44	28.70
Reduction to	62° F.		- 63.25 - 62.12	- 55 82 - 54 93	- 56°03 - 52°09	- 56.46 - 54.71	- 58°79 - 59°29	- 58.79 - 58.79	- 30-94 - 47-95	- 50.52 - 47.52	- 51.27	- 52°64 - 53•75
d ralues of nd A-D	in <i>m</i> .y		14.1851 1581-40	1648 o2 1563 57	1651.09 1569.02	1650°47 1568°13	18-121-99	1579.75	1359'64. 1559'64	1646.55 1564.44	1565.99 1649.16	1653 · 16 1574 · 57
Mean observe $I_S - D u$	in terms of G	Jime	1372.26	1430-06 1356-78	1432.73	1432°19 1360°7,4	1366.69 1435.96	1437-30 1370 82	1427-18	1428.79	14.31.05	1366+33
urea	Bur		64.98 64.85	64.63 64.52	68.49 49.49	15.tg 99.tg	64.77 64.72	82.49 22.49	64.40 64.20	64 38 64 18	6+.+9	64 - 48 64 - 42
Corrected i temperat	Air space		65°43 65°10	£9.†9 26.†9	65.tg	65 os 64 68	65.03 65.03	65 - 43 64 - 98	64.73 64.13	64 · 58 64 · 30	64-63 64-63	57.49 57.75
Mean	Room		o6. Ŝĝ	00.Sy	\$1.29	o£.ŝg	42.40	og. 59	02.19	06.19	65.10	65.45
c	887 		~ ~	- A	- ² 4	-° <	- [°] <	- A	<	- [°] <	- 4	- ^{s,} e
f observers	West end	-	Н. М. С.	Н. П. Т.	н . м. с.	н. п.	Н. П. Т.	н . м. с.	Н . П. Т.	Н . М. С.	н . ч. т.	Н . М. С.
Position of	East end		Н. Н. Т.	Н, М. С.	н. н. т.	н. м. с.	Н. М. С.	н. п. т.	н. м. с.	Н. Н. Т.	Н. М. С.	Н . Н. Т.
	<u>. </u>		19	20	20	20	30	50	53	23	53	53
	Dat	1906	Nov.	=	:	5	=	=	÷	Ŧ	:	2
	let et		11	12	EI	1#	15	16	17	18	19	20

THE BAR COMPARISONS

80.82 *m.y* 64°-56 F.

Mean value of $I_S - A$ (micrometer heads turned towards each other) Mean temperature **TABLE 1X.—Abstract of comparisons between A and 1**^s with deduced results—(Contd.). (Micrometer heads turned away from one another).

80.53 51.13 t9.88 80.64 66.08 86.28 85.44 **∀** ∣ 62° F. 20.62 ₹9.18 10.11 ų.m at <u>_</u>~ 5 Reduction t 62° F. 29.50 29.50 28.02 21.18 30.16 17.22 18-89 14-89 96-81 36.61 20-27 33 63 62 7 ŝ 2.3 . 62 37. 38.90 36. 11 + + + 1 + + 1.1 + + + + + + + • + g 773.95 850.52 728-13 812-10 50. †62 80. †12 710.79 777.80 858.50 68.867 794.30 704 05 785 13 18.111 725-11 806-81 28.112 y.n Mean observed values $D - I_S$ and D - A.⊒ terms of G 616.79 688.52 96.442 46.429 to.822 617.72 688-46 617°75 689°25 62.189 16.019 60.809 631.83 704.70 t9.619 80.689 66.4/9 12.629 11.00/ divns. Ξ. 63.39 63.24 63°43 63°30 63°70 63°68 63°75 63°70 62.94 62.87 63 32 63 43 63.41 63.30 61.32 61.32 86.29 12.19 50.19 10.89 Bar Corrected Mean temperature Air space 63.68 63.53 63.85 63.63 63.43 63.43 80.tg Eo.tg 63°04 63°38 63°08 63°43 63.28 63.83 63.48 64.18 61.25 62.08 61-38 62-13 5t.tg Room 64.75 64.70 <u>50.5</u>9 £6.E9 64.25 94.13 50.89 08.89 64.65 Ваг ~~< ~~ < ~~~ **<** -[°] • ~~< _∾ **∢** <u>~</u>~ ~~ < <u>~</u>~ ~~ < West End м. с. н. т. e. F c, E. Ö Ö H M. C. ×. Ħ. Ħ X. Ħ Ħ. Ħ. Position of observers Ħ. Ħ. щ Ħ H. H. Ħ. Ħ Ħ. Ħ. East end ei c, c, ರ M. C. H. H. T. ÷. Ċ, Ŀ. H. H. T. Н. М. H. M. Ä П. Н. Ħ. H. Н. М. н. Ħ. Ħ. Ħ. . 24 27 24 2 S 22 ន 25 26 28 Date 1908 Nov. . 2 2 : 2 2 = = 2 No. of Bet 21 22 33 2 33 26 5 28 6 8

OF 1907 AND 1908.

81.44 m.y 62°·91 F.

Mean value of 1g – A (micrometer heads turned away from one another) Mean temperature 31

No. of set	Mean temperature of Bars I _B and A	Value of $B_B - A$	No. of set	Mean temperature of Bars I _S and A	Vulue of I _S – A
1	6°5. 24	m.y m.y	11	64.92	<i>m.y</i> 81 86
2	65.20	187-23	12	64.58	83.56
3	65+48	196-14	13	64.22	78.13
4	65.49	193-29	14	64 · 59	80.59
5	65.03	190.12	15	64.75	80 . 32
6	65.00	193-71	16	64.28	78 • 4 2
7	65.11	100.00	17	64 · 30	82.07
8	64.71	194.01	18	64 · 28	79.11
9	64-61	188.66	19	64 · 47	85.44
10	64-65	192.36	20	64.45	78.70
31	59'71	197-13	21	63.32	79.02
32	59.78	103.31	22	63.37	80.39
33	60×32	191,00	23	63-69	81 62
34	60 ' 42	198.76	24	63.73	77.01
35	57 . 28	197.73	25	62.91	82.98
36	57-42	192.67	26	62.97	80.23
37	58.00	196.10	27	63.38	83.12
38	58.13	190-40	28	63.46	85.44
39	5914	198-37	29	61-13	83.64
40	59' 17	189152	30	61 * 22	80.64

TABLE X.—Values of $I_B - A$ and $I_S - A$ reduced to 62° F. as determined at Dehra, Nov.—Dec., 1908.

	I _B — A and Temperature	I _N — A and Temperature
Mean value for temperatures below 62	194 · 50 <i>m</i> .y	82·14 m.y
Corresponding mean tempera- ture	58 [°] 94 ₽.	61[°]18 F.
Mean value for temperatures above 62°	192 [.] 27 m.y	81 [·] 02 m.y
Corresponding mean tempera- ture	65 [°] 05 F.	64[°]03 Г.
General mean value	193 3 8 m.y	81 · 13 m.y
General mean temperature	61 [°] 99 F.	63 [°] 74 F.

TABLE XI.—Mean values of $I_B - A$ and $I_S - A$ reduced to 62° F. from Dehra observations, Nov.—Dec. 1908, as found by the second series of observations.

APPENDIX No. 1

The following letter was received from the Director of the Bureau International des Poids et Mesures, Breteuil Sévres, July, 1908:-

A detailed report of the operations will be sent in a short time. The observations were made at temperature between 17° and 18° (Centigrade). Bar **A** at $17^{\circ}5$ is $3048 \cdot 026$ mm. The value reduced to 62° F. becomes $3047 \cdot 996$ mm.

The value given in Vol. I of the Indian Survey is

3·333,318,86 yds.,

which using the equivalent determined at the Bureau International gives $3047 \cdot 984$ mm.

The difference is extremely small, taking into consideration the distant date of the determination of the length of the bar, the difficulty of intersecting the unsatisfactorily defined dots and finally the conversion, first, to the yard and then to the metre by an intermediate series.

Guillaume.

The length of bar \mathbf{A} , as determined at Sévres, expressed in yards is accordingly $3 \cdot 333,332$.

The corresponding lengths of I_{s} and I_{B} determined from the observations of Nov. 1907—Jan. 1908 are as follows:—

 $I_s = 3.333,415$ yds. $I_B = 3.333,529$ yds.

The later observations of Nov.-Dec. 1908 were not used as the thermometer corrections had not been redetermined.

All the above are for temperature 62° F.

THE BAR COMPARISONS

APPENDIX No. 2

Bar A Bar Is Set End of [Difference Difference Difference Difference No. Bar i Air space Bar Air space Bar Bar--Air E - WBar-Air E-W temperature temperature temperature temperature for Bar space space for Bar :8°.60 58°38 1 Е 58°18 - 0. , , 38-30 -0.13 w 58.10 59135 -1.16 58 70 +0.10 58.33 -0.12 -0:37 2 R 58.56 -0.04 59:50 50.04 58:33 -0.25 w -8-10 59115 +0.10 58.45 -0.75 58 80 -0.35 -0.13 3 \$8.30 \$8.00 -0:30 58.35 58.25 -0.10 w 58 15 58 10 -0.05 -0.10 38115 58.40 + 0' 25 -0.15 4 :8.10 Е 57:96 -014 58130 58:28 - 0 · 0 2 w \$8 65 58.01 -0.01 - 0.01 58 40 58.39 -0.01 -0.11 5 R 58.20 58-33 - 0.37 58.70 58.40 - 0130 58.75 W 58 23 -0'52 + 0.10 \$8.55 58.40 -0.00 -0.00 6 ы :8:30 58.14 +0.14 58.00 58:43 -0.42 w 58 28 59:15 -0.87 +0.10 58.00 58:54 -0.30 -0.11 7 57.85 Е 57 89 +0.01 38.10 58.04 -0.06 w 57.95 57.79 -0.10 +0.10 :8 08 58-14 + 0.06 - 0.10 8 E 58.05 57.75 -0.30 58 25 58.00 -0.25 w 58.15 57174 -0'11 + 0 . 0 1 \$8.20 58.10 -0.10 -0.10 9 Е 58.10 57:95 -015 :8.60 :8.0: -0.55 w 57 86 38:55 -0.60 +0.00 \$8 10 58'10 +0 00 -0.14 10 \$8 30 E :8.0: \$8.25 58 00 -0.25 -0.10 w 58.70 58.05 -0.65 :8 . 28 0.00 \$8:33 -0.02 -0.10 11 57 95 E 57.64 -0.31 57:65 + 0 . 10 57°75 57°84 w 57 65 57:43 -0'22 + 0 . 21 57.88 -0.04 -0.00 12 Е 57195 57:45 -0:50 :8'18 57:79 -0.30 w 38.05 57-84 57:49 -0.40 -0.01 57.85 -0.01 -- 0.03 57195 13 Е 57:69 -0.26 58:45 57.88 -0'57 w 58 55 57.64 + 0 24 -0.01 + 0.05 57:70 57 94 -0.00 14 E 58 · 0 = 57:89 -0.10 58:35 -0.10 57.95 w 58.45 58 10 57174 -0.71 + 0115 57 95 -0.15 0.00 15 Е 57115 57 29 +0 14 57:50 + 0.10 57:40 w 57.65 +0.00 -0.01 57:20 -0145 - 0.01 57155 57:54 16 Е 57.88 -0.38 57 45 57150 57:30 -0'15 W -0.01 +0.10 - 0.20 -0.02 57 75 57114 57.75 57:55 17 57.50 E 57:09 +0.10 57:85 57155 -0:30 W 57 64 57 80 57175 57138 -0.37 +0.31 -0.10 -0.00 18 ĸ 57.60 -0.30 58.10 57195 57155 -0.10 57 . 65 w + 0.01 \$7 63 -0.32 -0'03 57151 -014 57 95 19 Е \$6.83 56.00 - 0 . 30 -0.22 57'20 57 05 w \$6.95 56 73 + 0 10 56:90 - 0 20 0.00 -0.35 57:10 20 Е 56:96 -0.10 57 25 56 95 -0.30 57:15 w 56-80 57:45 -0.65 +0.10 57115 \$6.00 -0.10 -0.04

Analysis of temperature readings during the comparisons of bars 1, and A, Nov. 1907—Jan. 1908.

OF 1907 AND 1908.

APPENDIX No. 2--(contd.)

·	Bur A					Bur I _S			
Set No,	End of Bar	Air space temperature	Bar temperature	Difference Bar— Air space	Difference E—W for Har	Air space temperature	Bar temperature	Difference Bar—Air space	Difference EW for Bar
21	E W	56-65 56-75	56° 48 56 41	- 0 · 17 - 0 · 34	+0.02	57°10 56°75	56°75 56°85	- 0° 35 + 0° 10	-0.10
22	E W	56 65 56 75	56+56 56+46	- 0 ' 09 - 0 ' 29	+ 0 · 10	57°05 57°00	56 78 56 78	$ \begin{array}{c} -0.27\\ -0.22 \end{array} $	0.00
23	E W	56-95 57-15	56+89 56+70	- 0 ° 0() - 0 ° 45	+ 0,119	57°25 57°10	56+86 56+85	-0:39 -0:25	+0.01
24	E W	57145 57145	56-88 56-78	$- \circ 27 \\ - \circ 37$	+0.10	57°25 57°15	56-89 56-86	-0.36 -0.29	+0.03
53	E W	64°10 64°03	63-81 63-80	$ \begin{array}{c} -0.20 \\ -0.23 \end{array} $	+0.01	64.20 64.10	64°03 64°09	- 0' 17 - 0' 01	- 0 · 06
54	E W	64°00 64°15	63*91 63*80	-0.09 -0.35	+0.11	64120 64110	64≛00 64≛10	- 0 ° 20 0 ° 00	-0.10
55	E W	65 90 65 75	65°03 64°93	- 0 87 - 0 82	+0.10	63,55 65,45	64+90 65+11	-0.65 -0.34	-0.51
56	E W	65190 65195	65 08 64*96	- 0 · 82 - 0 · 99	+ 0 ' 1 2	66+15 66+15	65°25 65°31	-0.00 -0.20	- o · o6
57	E W	68 95 68 93	68:50 68:45	- 0 . 10	+ 0 · 05	69+15 68+95	68 · 50 68 · 63	- 0 65 - 0 32	-0.13
58	E W	68 95 68 95	68+69 68+75	- 0 · 26 - 0 · 20	- o · o6	69°15 68°75	68+75 68+95	- 0, 10 - 0, 10	-0.50
59	E W	68 95 68 75	68 78 68 75	- 0 · 17 0 · 00	+ 0 . 03	69-15 68+90	68+83 68+95	0' 32 + 0' 05	- 0 ' 1 2
60	E W	68 95 68 95	68+90 68+78	- 0 · 05 - 0 · 17	+ 0 ' 1 2	69°00 69°00	68+89 68+95	- 0° 26 - 0° 05	-0.00
61	E W	64+70 65+05	64+88 64+98	+ 0 · 18 - 0 · 07	-0.10	65 05 63 10	65+14 65+35	+ 0 ° 09 + 0 ° 25	-0'21
62	R W	64:00 65:05	64+81 64+83	- 0 ' 00) - 0 ' 2 2	- 0 ' 02	65+20 64+95	65-13 65-23	-0.07 +0.28	-0.10
63	E W	65-10 65-05	64°91 64°90	- 0, 10 - 0, 12	+ 0 . 01	65 00 65115	65+ 00 65+15	0.00	- 0 ' 15
64	E W	05100 04155	64-86 64-80	-0.14 +0.25	+ o · of	65 · 20 65 · 00	65°00 65°15	- 0 · 20 + 0 · 15	- 0 . 12
65	E W	65.00 64.95	64175 64175	- 0 · 25 - 0 · 20	0.00	63115 65150	65.00 64.99	- 0' 15 - 0' 51	+ 0.01
66	R W	65 00 65 15	64-80 64-75	- 0 · 20 - 0 · 20	+ 0 • 05	63.10 63.10	65+00 64+99	-0.11	+ 0.01
67	E W	65-70 65-65	63.23 65.19	- 0 · 16	+ 0 . 01	65155 65160	65+25 65+38	-0.30 -0.32	-0.13
68	E W	65 90 65 75	65+35 65+19	- 0, 55 - 0, 56	+ 0 16	65+95 65+35	65135 65143	o fio +o∙o8	- o`08
69	W W	65195 63195	65-74 65-60	- 0° 35	+0.11	66.00	65 80 65 84	- 0 · 20 - 0 · 16	-0.01
70	E W	65°90 66°03	65+63 65+56	- 0 · 27 - 0 · 19	+0.07	66+56 65+80	65+81 65-90	-0.34 +0.10	- 0 ' 09

Analysis of temperature readings during the comparisons of bars $|_{s}$ and A, Nov. 1907—Jan. 1908 (contd.).

THE BAR COMPARISONS

APPENDIX No. 3

		Bar /	4	Bar I _S				
Set No	Mean air space temperature	Change: set to set	Mean bur temperature	Change: set to set	Mean air space temperature	Change: set to set	Mcan bar tempera- ture	Change: set to set
1	58.98		58-28		58150		5 ⁸ ·26	
2	59,33	+ 0135	58.48	+ 0 . 30	58.93	+0.43	58.39	+ 0.13
3	58.23	-1.10	58.02	-0.43	58 - 25	- 0 · 68	58.33	-0.06
4	58.38	+0.12	57198	-0.01	58.32	+0.10	58.34	+ 0.01
5	58.73	+0.32	58 28	+ 0 . 30	58-63	+ 0 . 28	58.43	+0.00
6	58.73	0.00	58.36	+0.08	58.90	+ 0 ' 27	58-48	+0.02
ī	57 ' 90	- o · 8,3	57.84	-0.52	58.00	- o · 8 i	58.00	- o · 39
8	58.10	+ 0 * 20	57.75	-0.00	58.23	+0.14	58.05	-0.04
9	58.33	+0'23	57:90	+ 0 * 1 5	58135	+ 0 ' 1 2	58.12	+0.02
10	58.30	+0.12	58.05	+ 01 15	58.29	- o · o6	58.10	+0.02
11	57.80	-0.20	57*54	-0.21	57.77	— O [·] 5 ²	57.79	- o . 40
12	58.00	+ 0 . 30	57+47	-0.01	58.02	+ 0 . 2 2	57.81	+ 0 . 05
13	58+25	+ 0 . 25	57.67	+ 0 • 20	<u>5</u> 8±08	+0.00	57.91	+ 0' 10
14	58-25	0.00	57.82	+ 0 . 1 2	58.23	+ 0.12	57.95	+0.01
15	57.40	-0.85	57:25	-0.57	57.48	-0.75	57.52	-0.43
16	57.60	+ 0 • 20	57.22	-0.03	57.82	+0.34	57.53	+0.01
17	57.67	+0.02	57.54	+ 0 ' 32	57.83	+ 0.01	57.60	+0.02
18	57×80	+0.13	57:53	-0.01	58.03	+ 0 ' 20	57.62	+ 0 ' 02
19	57.00	- o · 80	56.78	-0.12	\$7.15	-o·88	56.00	- 0 [.] 7 2
2 0	57:30	+0.30	56.88	+0.10	57 20	+0.02	56.92	+0.02
21	56.20	- o · 60	56.45	-0.43	56 93	-0.21	56 · 80	-0.12
22	56.20	0.00	56 - 51	+ o . où	57:03	+0.10	56 78	-0.05
23	57:05	+ 0 . 35	56.29	+ 0 . 28	57118	+ 0 . 1 5	56.80	+ o · o8
24	57115	+0.10	56.83	+0.01	57 ' 20	+ 0 ' 02	56.88	+ 0 . 0 2
53	64.02		63.81		64115		64.06	
54	64.08	+0.01	63.86	+ 0.03	64.15	0.00	64.05	0.01
55	65-83	+1.75	64.98	+ 1,12	65.50	+1.35	6 <u>≴</u> ∶or	+0.00
5G	65.93	+0.10	65.02	+0.04	66+13	+0.63	65 28	+ 0 · 27
57	68 90	+ 2 . 9 .	68+47	+ 3 45	69.05	+ 2'92	68 - 57	+ 3 20
58	68 95	+0.02	68 - 7 3	+ 0 . 2 5	68195	-0.10	68·85	+ 0 * 28

Analysis of temperature readings during the comparisons of bars l_s and A, Nov. 1907—Jan. 1908.

OF 1907 AND 1908.

APPENDIX No. 3-(contd.)

I	Ī	J	Bar A	Bar I _S				
Set No.	Mean air space temperaturo	Change: set to set	Mean bar tomperature	Change: set to set	Mean air space temperature	Change: set to set	Mean tar tempera- ture	Change: set to set
59	68°85	-0.10	68 ^{°.} 77	+ 0.05	69°03	+0.08	68.89	+0.04
60	68.95	+0.10	68.84	+0.02	69°08	+0.02	68.92	+0.03
61	64.88	-4.02	64.93	-3.01	65.08	-4.00	65.25	-3.67
62	64.98	+0.10	64.82	-0.11	65.08	0.00	65.18	-0.02
63	65.08	+0.10	64.90	+ 0 ' 08	65.08	0.00	65.08	-0.10
64	64.78	-0.30	64.83	-0.01	65.10	+0.05	65.08	0.00
65	64.98	+ 0 ' 20	64.75	-0.08	65 33	+0.53	65.00	-0.08
66	65.08	+0.10	64.78	+0.03	65.10	-0.53	64.99	-0.01
67	65.68	+0.60	65.31	+ 0 ' 43	65 - 58	+0.18	65.32	+ 0.33
68	65.83	+0.12	65 · 27	+0.00	65-65	+0.02	65 . 39	+0'07
69	65 95	+0'12	65.67	+0.40	66 . 00	+ 0 ' 35	65.82	+0.43
70	65+98	+0.03	65.20	-0.08	65.98	~0'02	65.86	+0.04

Analysis of temperature readings during the comparisons of bars I_s and A, Nov. 1907—Jan. 1908 (contd.).